

#LECTURE 16 : Mutable Algorithms I

> fib :: Int → Integer

> fib n = loop n 0 1

> where

> loop 0 x y = x

> loop n x y = loop (n-1) y (x+y)

> fib' :: Int → Integer

> fib' n = runST \$ do {

> rx ← newSTRef 0 ;

> ry ← newSTRef 1 ;

> let loop 0 = do {

> x ← readSTRef rx ;

> return x ; }

> loop n = do

> { x ← readSTRef rx ;

> y ← readSTRef ry ;

> writeSTRef rx y ;

```

> writeSTRef ry (x+y);
> loop (n-1) ; }
> loop n ;

```

State transformer
state return value.

runST :: (forall s. ST s a) -> a

newSTRef :: a -> ST s (STRef s a)

readSTRef :: STRef s a -> ST s a

writeSTRef :: STRef s a -> a -> ST s ()

return :: a -> ST s a

newArray :: $\mathbb{I} \times i \Rightarrow (i, i) \rightarrow a \rightarrow \text{ST } s (\text{STArray } s \ i \ a)$
↓ index range
↓ default

readArray :: $\mathbb{I} \times i \Rightarrow \text{STArray } s \ i \ a \rightarrow i \rightarrow \text{ST } s \ a$

writeArray :: $\mathbb{I} \times i \Rightarrow \text{STArray } s \ i \ a \rightarrow i \rightarrow a \rightarrow \text{ST } s \ ()$

minfree xs returns the smallest free natural number in xs.

minfree [3, 2, 0, 1, 6, 8, 7]

↓ checklist xs

[✓ ✓ ✓ ✓ × × ✓ ✓ ✓]
0 1 2 3 4 5 6 7 8 ...

↓ takeWhile id

[✓ ✓ ✓ ✓]

↓ length

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minfree :: [Int] → Int

minfree xs = length (takeWhile id (checklist xs))

checklist :: [Int] → [Bool]

checklist xs = runST \$ do

ays ← newArray (0, m-1) False :: ST s (STArray s Int Bool)

sequence [writeArray ays x True | x ← xs, x < m]

xs' ← getElements ays

return xs'

where

$m = \text{length } xs$

extracts
all elements.
↓

$\text{getElements} :: [x] \Rightarrow \text{STArray } s \, i \, a \rightarrow \text{ST } s \, [a]$

> class Hashable a where

> hash :: a → Int

hash "Hell" = 73

hash "World" = 42

hash "algorithm" = -4721

hash "purple" = 73

↖ hash collision

nub removes duplicates (not necessarily stable).

nub [3, 2, 5, 3, 3, 5, 8]

=

[3, 2, 5, 8]

hash 3 = 42

hash 2 = 0

hash 5 = 255

hash 8 = 42

[Int]

1C

#0 : ~~[]~~ 2 : []

#1 : []

#2 : []

:

#42 : ~~[]~~ 3 : ~~[]~~ 8 : 3 : []

:

#255 : ~~[]~~ 5 : []

]1